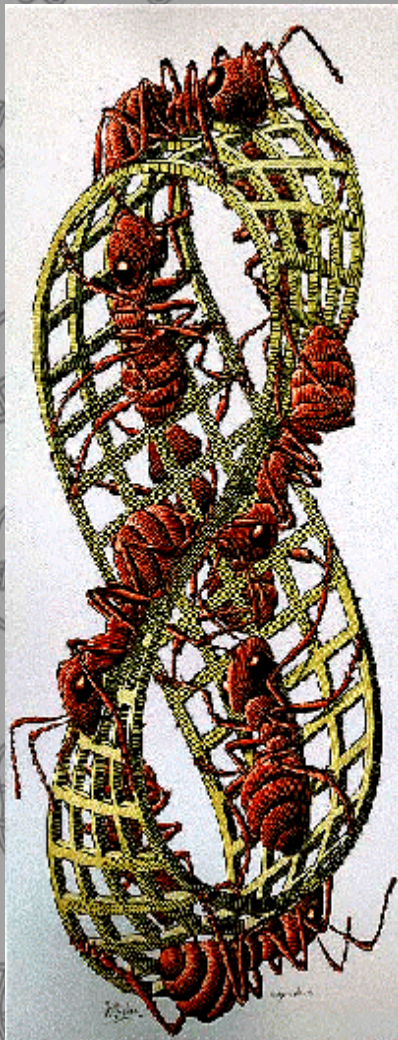


# 2016 Winter TAPU Workshop on Knots and Related Topics



15(Mon)-16(Tue) February, 2016

Natural Science Building, Room 219  
College of Natural Sciences  
Kyungpook National University

Organizers:  
YongjuBae(KNU, Chair)  
Sang YoulLee(PNU)

Sponsors:  
BK21+ Next CMC, KNU  
National Research Foundation of Korea  
BK21+ CMRE, PNU

Contact: YongjuBae  
T E L : 82-53-950-6307. FAX : 82-53-950-6306  
E-mail : [ybae@knu.ac.kr](mailto:ybae@knu.ac.kr)

# SCHEDULE

**15(Mon) February 2016**

**09:25-09:30**

**Opening**

**09:30-10:20**

**Chair :Y. Bae**

**Sang Youl Lee (Pusan National University)**

**The Quantum  $A_2$  Invariant for Virtual Tangled Trivalent Graph Diagrams**

**10:40-11:10**

**Chair :Y. Bae**

**Myeong-Ju Jeong (KAIST)**

**An Even Polynomial and Bridge Diagrams**

**11:20-11:50**

**Chair :Y. Bae**

**Seogman Seo (Kyungpook National University)**

**Virtual Links and Graphs**

**11:50-13:30**

**Lunch**

**13:30-14:30**

**Chair :S.Y. Lee**

**Kengo Kawamura (Osaka City University)**

**Modification of Quandle (Co)Homology Groups for Immersed Surface-knots**

**Byeorhi Kim (Kyungpook National University)**

**On Finite Quandles and Their Inner Automorphism Groups**

**Jihee Kim (Pusan National University)**

**Index Polynomials for Gauss Diagrams of Virtual Links and Utilization**

**Suhyeon Jeong (Pusan National University)**

**Parities and an Odd Polynomial Invariant for Virtual Links and Utilization**

**14:50-15:40**

**Chair :S.Y. Lee**

**Myoungsoo Seo (Kyungpook National University)**

**On the Writhe of Periodic Virtual Knots**

## Colloquium

**16:00-16:50**

**Chair :Y. Bae**

**Seiichi Kamada (Osaka City University)**

**On Braid Description of Surface-links in the 4-space**

**17:00 -**

**Free Discussion and Dinner**

## **16(Tue) February 2016**

**09:30-10:20**

**Yukio Matsumoto (Gakushuin University)**

**Riemann Surfaces and Crystallographic Groups**

**Chair :C.-Y. Park**

**10:40-11:30**

**Sangyop Lee (Chung-Ang University)**

**Twisted Torus Knots**

**Chair :C.-Y. Park**

**11:40-13:30**

**Lunch**

**13:30-14:30**

**Kaori Hasegawa (Osaka City University)**

**Cocycle Invariants of the Dihedral Quandle of Order 6**

**Chair :M. Seo**

**Seonmi Choi (Kyungpook National University)**

**On Finite Quandles and Rack Homology Groups**

**Hyeran Cho (Pusan National University)**

**Obtaining a Presentation of Knot Groups by Wirtinger Presentation**

**Geunyoung Kim (Pusan National University)**

**An Index Definition of Parity Mappings of a Virtual Link Diagram and Utilizations**

**14:50-15:40**

**Akio Kawauchi (OCAMI, Osaka City University)**

**On a Cross-sectional Link of an Immersed Sphere-link in 4-space**

**Chair :Y. Bae**

**16:30 -**

**Free Discussion and Dinner**

# ABSTRACT

**Hyeran Cho (Pusan National University)**

## **Obtaining a Presentation of Knot Groups by Wirtinger Presentation**

Abstract: We introduce Wirtinger presentation which is a method to find a group presentation of a knot group and consider some of its examples given in [Gerhard Burde and Heiner Zieschang, Knots, 32-37pp.].

**Seonmi Choi (Kyungpook National University)**

## **On Finite Quandles and Rack Homology Groups**

Abstract: Let  $Q$  be a finite set and let  $\{*_1, *_2, \dots, *_m\}$  be the set of all quandle operations of  $Q$ . The product  $*_{ij}$  of two quandle operations  $*_i$  and  $*_j$  can be defined by  $x *_i *_j y = (x *_i y) *_j y$  for every  $x, y \in Q$ . In this talk, we will introduce an algebraic structure on the set  $\{*_1, *_2, \dots, *_m\}$  of quandle operations and study their rack homology groups.

**Kaori Hasegawa (Osaka City University)**

## **Cocycle Invariants of the Dihedral Qualegebra of Order 6**

Abstract: A qualegebra is a quandle with a multiplication. By using a qualegebra, V. Lebed defined colorings and cocycle invariants of spatial trivalent graphs. We consider the qualegebra obtained from the dihedral group of order 6. We show some examples of shadow 2-cocycles of the qualegebra, and calculate cocycle invariants for some spatial trivalent graphs.

**Myeong-Ju Jeong (KAIST)**

## **An Even Polynomial and Bridge Diagrams**

Abstract: I have introduced bridge diagram of a virtual knot diagram. For each virtual knot diagram, we can associate a bridge diagram obtained by introducing a bridge with a sign for each crossing. I will introduce a polynomial invariant of virtual knots by considering weights of a bridge. It gives us a Vassiliev invariant distinguished from the affine index polynomial and the zero polynomial.

**Suhyeon Jeong (Pusan National University)**

## **Parities and an Odd Polynomial Invariant for Virtual Links and Utilization**

Abstract: We introduce the odd Jones-Kauffman polynomial of virtual link diagrams by using the parity of virtual link diagrams given in [Y. H. Im and K. I. Park, A parity and a multi-variable polynomial invariant for virtual links, J. Knot Theory Ramifications 22(13) (2013), Article ID: 1350073, 18pp.], which are different from the original Jones-Kauffman polynomial.

**Seiichi Kamada (Osaka City University)**

## **On Braid Description of Surface-links in the 4-space**

Abstract: We discuss about braid presentations of surface-links in the Euclidean 4-space. First we introduce the classical dimensional case. Alexander and Markov's theorems state that every link in the Euclidean 3-space can be presented as a closed braid (the closure of a braid), and such a braid presentation is unique up to braid ambient isotopy, conjugation and stabilization. An analogous

result holds for surface-links in the 4-space. Every surface-link can be presented as a closed surface-braid and such a braid presentation is unique up to braid ambient isotopy, conjugation and stabilization.

**Kengo Kawamura (Osaka City University)**

### **Modification of Quandle (Co)Homology Groups for Immersed Surface-knots**

Abstract: An immersed surface-knot is an oriented closed connected surface generically immersed in a 4-space. In this talk, we introduce a modification of quandle (co)homology groups which is closely related to diagrams of immersed surface-knots.

**Akio Kawauchi (OCAMI, Osaka City University)**

### **On a Cross-sectional Link of an Immersed Sphere-link in 4-space**

Abstract: The torsion Alexander polynomial and the local signature of a cross-sectional link of an immersed 2-link are investigated from the viewpoint of how to influence to the immersed 2-link. It is shown that the torsion Alexander polynomial of a symmetric middle cross-sectional link of a ribbon 2-link is a topological invariant of the ribbon 2-link. A generalization to an immersed 2-link is also shown.

**Byeorhi Kim (Kyungpook National University)**

### **On Finite Quandles and Their Inner Automorphism Groups**

Abstract: Let  $Q$  be a finite set. Let  $*$ <sub>1</sub> and  $*$ <sub>2</sub> be two quandle operations on  $Q$ . Then the product  $*$ <sub>1</sub> $*$ <sub>2</sub> :  $Q \times Q \rightarrow Q$  defined by

$a *_{1} *_{2} b = (a *_{1} b) *_{2} b$  for all  $a, b \in Q$ , is not a quandle operation in general.

In this talk, we will study the relationship between the inner automorphism groups  $\text{Inn}(Q, *_{1})$ ,  $\text{Inn}(Q, *_{2})$  and  $\text{Inn}(Q, *_{1} *_{2})$  in the case that  $(Q, *_{1} *_{2})$  is a quandle.

**Geunyoung Kim (Pusan National University)**

### **An Index Definition of Parity Mappings of a Virtual Link Diagram and Utilizations**

Abstract: H. Dye defined the parity mapping for a virtual knot diagram, which is a map from the set of real crossings of the diagram to  $\mathbb{Z}$ . The notion generalizes the parity which is studied extensively by V. Manturov. The mapping induces the  $i$ -th writhe  $w_i \in \mathbb{Z} \setminus \{0\}$  which is an invariant of the representing virtual knot. She applied the parity mapping to introduce a gradeto the Henrich  $SS$ -invariant for a virtual knot, and showed that the invariants are Vassiliev invariants of degree one. Following it, we define the parity mappings for a virtual link diagram, and define the similar invariants as above for a virtual link by using the parity mappings.

**Jihee Kim (Pusan National University)**

### **Index Polynomials for Gauss Diagrams of Virtual Links and Utilization**

Abstract: We introduce the index polynomial for Gauss diagrams corresponding virtual links, which is easier to calculate than that of virtual links.

**Sangyop Lee (Chung-Ang University)**

### **Twisted torus knots**

Abstract: Twisted torus knots are obtained by adding full twists to some parallel strands of torus knots. We will discuss some properties of these knots.

**Sang Youl Lee (Pusan National University)**

**The Quantum  $A_2$  Invariant for Virtual Tangled Trivalent Graph Diagrams**

Abstract: A tangled trivalent graph diagram is an oriented link diagram possibly with some trivalent vertices whose incident edges are oriented all inward or all outward. G. Kuperberg derived an inductive, combinatorial definition of a polynomial-valued invariant, called the quantum  $A_2$  invariant, with values in the ring of one variable integral Laurent polynomials, which is an invariant for regular isotopy of tangled trivalent graph diagrams.

In this talk, I would like to talk about an extension of the quantum  $A_2$  invariant to virtual tangled trivalent graph diagrams and some applications.

**Yukio Matsumoto (Gakushuin University)**

**Riemann Surfaces and Crystallographic Groups**

Abstract: A Riemann surface is a closed surface with a complex structure, while a crystallographic group is an isometry group acting on a Euclidean space  $\mathbb{E}^n$  whose translation subgroup forms an  $n$ -dimensional lattice. For example, a so-called wall paper group is a two dimensional crystallographic group. This talk will report our recent discovery that certain crystallographic groups on  $\mathbb{E}^{3g-3}$  naturally arise from a Riemann surface of genus  $g$ .

**Myoungsoo Seo (Kyungpook National University)**

**On the Writhe of Periodic Virtual Knots**

Abstract: In 2014, Satoh and Taniguchi defined the  $n$ -th writhe of a virtual knot for each non-zero integer  $n$  and proved that the  $n$ -th writhe is a generalization of the index polynomial and the odd writhe polynomial. In this talk, we will review the  $n$ -th writhe of a virtual knot for each non-zero integer  $n$  and discuss some properties of the  $n$ -th writhe of periodic virtual knots.

**Seogman Seo (Kyungpook National University)**

**Virtual Links and Graphs**

Abstract: In this talk, I introduce a correspondence between virtual links and graphs which is given by Jablan, Radović and Sazdanović in 2011. By using this correspondence, I would like to introduce new virtual link invariants derived from topological indices; The weiner index and the harary index.